

## Production-Distribution Coordination of Industrial Gases Supply-chains

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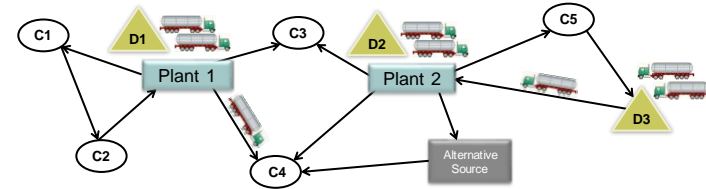
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## Background and Motivation

### Industrial Gases Supply-Chain

- ❑ Multiple Plants and Depots (located or not at plants)
- ❑ Multiple Products (*LIN, LOX etc.*) and Product Grades
- ❑ Over-the-fence, call-in and distributed customers (*some shared customers*)
- ❑ Storage facilities at production sites and customer locations

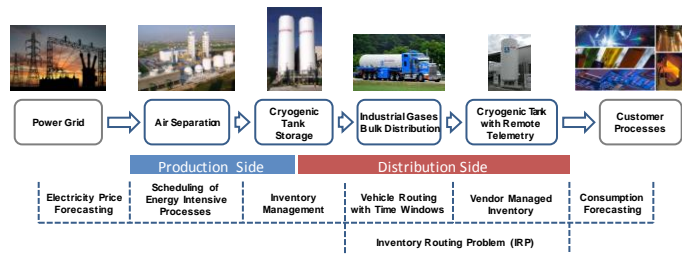


### Goal

To quantify and assess the savings associated with the **Production-Distribution Coordination at Operational Level** using an approximate model

## Background and Motivation

### Production and Distribution of Liquefied Industrial Gases



### Alternatives to reduce Distribution Side complexity:

- **Planned Delivery Forecast:**  
Amount of product delivered to customers given for each time interval.
- **Full Inventory Routing Problem:**  
No assumption on distribution side. The model determines when and how much product to deliver to each customer such that customer inventory constraints hold.

## Problem Statement and Main Assumptions

### Given

- Plants, Products, Operating Modes and Production Limits
- Daily Electricity Prices (off-peak and peak)
- Customers and their demand/consumption profiles
- Max/Min inventory at production sites and customer locations
- Alternative sources and product availabilities
- Depots, Truck availabilities and capacities, Distances
- Fixed Planning Horizon (usually 1-2 weeks)

### Decisions in each time period $t$

- Modes and production rates at each plant
- Inventory level at customer location and plants
- How much product to be delivered to each customer through which route

### Objective Function

- ❖ Minimize total production and distribution cost over planning horizon

### Main Assumptions – Distribution Side

- Two time periods per day (peak and off-peak) are considered
- Trucks do not visit more than 4 customers in a single delivery

# Mathematical Model (MILP)

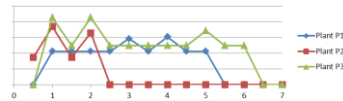


**Objective**

**Minimize total Production and Distribution Cost**

**Constraints on Production Side**

- Production Cost** = Fixed Start-up cost + Variable production cost
- Min/Max **Production Capacity** Constraints in each mode of operation
  - Logic Constraints** for switching between various modes of operation
  - Max/Min **Inventory limits** at the production sites
  - Plant Inventory Balance** Constraints
  - Demand satisfaction** for pick-up customers
  - Ad Hoc Production Models**  
To account for specific equipment configurations and production modes.



**Main binary variables**  
mode selection  
 $B_{pmt}$

# Mathematical Model (MILP)

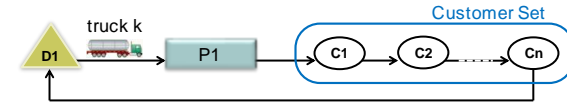


**Constraints on Distribution Side**

- Distribution Cost** = Cost of deliveries by trucks + purchases from competitors
- Max/Min **Inventory limits** at the customer locations
  - Customer Inventory Balance** Constraints
  - Truck Capacity** constraints
  - Material balance** constraints for product pick-up and delivery points
  - Max product purchase** limit from alternative sources

**Main binary variables**  
truck-customers association  
 $y_{kst}$   
truck-source association  
 $Y_{kpt}$

**Route = Depot + Plant + Customers**

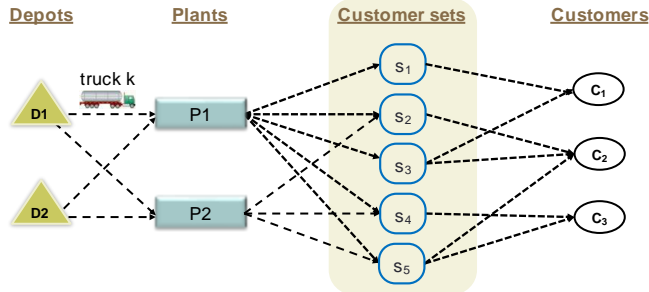


**Route Generation Algorithm** developed to obtain alternative routes for truck distribution.

# Supply-chain Example



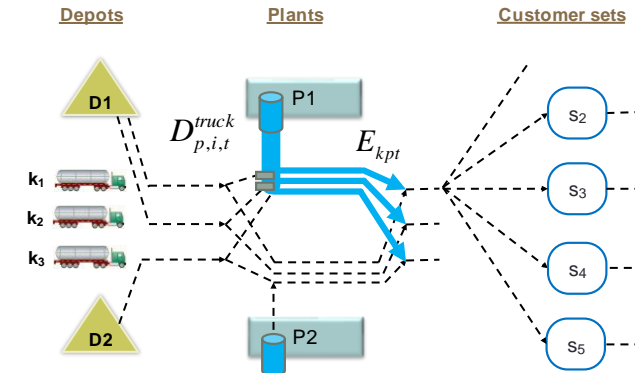
**Definition of Customer Sets:**



# Supply-chain Example



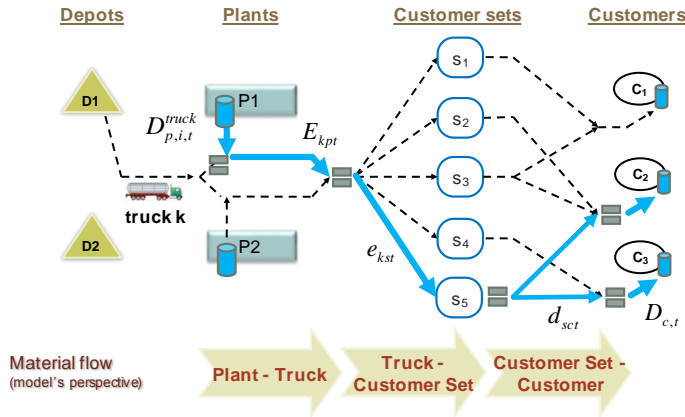
**Meaning of continuous variables to transfer products from plants to customers:**



## Supply-chain Example



Meaning of continuous variables to transfer products from plants to customers:



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## Industrial Size Test Case



- 4 Plants / Depots
- 2 products (LIN, LOX)
- 2-4 production modes for each plant
- 2 alternative sources
- 258 customers
- 14 time periods (peak and off-peak)
- 37 trucks (25 for LIN, 12 for LOX)
- Min/max inventory, distances, electricity prices, truck deliveries, etc.

Model Size	Binary variables	18,378
	Continuous variables	26,241
	Constraints	27,101

CPU results	Time	79 s
	Nodes	1,632
	Relative gap	0.1%

Good solutions found in few CPU sec.!!!

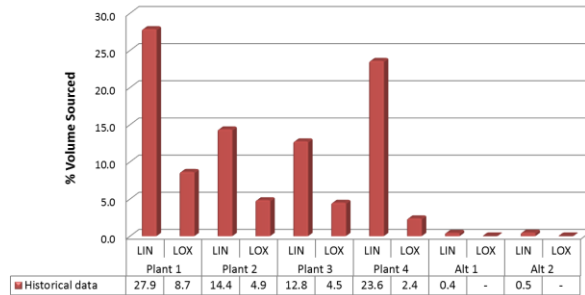
Models implemented with GAMS  
CPU results obtained with solver CPLEX 12.3

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## Industrial Size Test Case



Results are compared with historical data by fixing volume sourced from each plant.



### Historical Model:

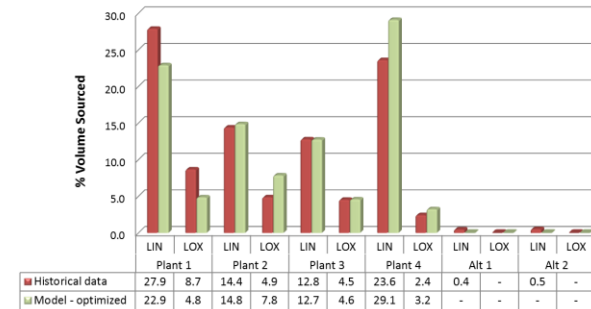
- Volume sourced is fixed to historical data.
- Production and distribution subproblems do not need to be solved simultaneously.
- Production subproblems can be solved for each plant.

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## Industrial Size Test Case – Results



Comparison of volume sourced: optimal model solution vs historical data.



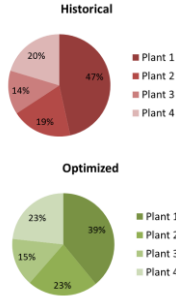
Optimal solution shifts production and distribution from plant P<sub>1</sub> to plant P<sub>4</sub>, mainly due to lower electricity costs at P<sub>4</sub>

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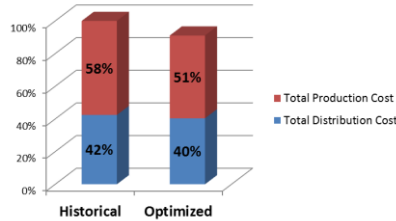
# Industrial Size Test Case – Results



Production cost % for each plant



Percentage of Total Historical Cost



$$\text{Savings} = \frac{[\text{Amount saved}]}{[\text{Historical model total}]} = 9\% \text{ per week}$$

# Improved Route Generation Algorithm



## Main Features:

- Exact distances among plants, depots, & customers obtained by GIS software.
- Route distances calculated using TSP method.
- Multiple parameters for each plant and product.
- Added routes to import product to plants (shut-down scenario)
- Alternative sort criteria to rank potential routes:
  - Distance (miles)
  - Logistics Ratio (\$ / volume delivered)



Route Generation Parameters													
RG_Parameters													
	p1	p1	p2	p2	p3	p3	p4	p4	comp1	comp1	comp2	comp2	comp3
	i1	i2	i1	i2	i1	i2	i1	i2	i1	i2	i1	i2	i1
Generate routes for this plant/product	x	x	x	x	x	x	x	x	x	x	x	x	x
Include all one-customer routes	no	no	no	no	no	no	no	no	no	no	no	no	no
Maximum customers visited	3	3	3	3	3	3	3	3	2	2	2	2	2
Maximum distance	400	400	400	400	500	500	500	500	500	500	500	500	500
Minimum filling ratio	70%	70%	70%	70%	70%	70%	70%	70%	70%	70%	70%	70%	70%
Maximum total routes	50	50	50	50	50	50	50	50	50	50	50	50	50
Minimum routes per customer	1	1	1	1	1	1	1	1	1	1	1	1	1
Limit routes per customer (0 = none)	2	2	2	2	2	2	2	2	2	2	2	2	2
Sort routes by:	Cost / Volume delivered (\$ / hact)												
Add routes to plants (fake customers)	<input type="checkbox"/>												

# Improved Route Generation Algorithm



## Progress Status, Statistics and Detailed Results

Progress		Statistics											
Iteration	Plant	p1	p1	p2	p2	p3	p3	p4	p4	comp1			
	Product	i1	i2	i1	i2	i1	i2	i1	i2	i1			
	Stage	all done	done	done	done	done	done	done	done	done			
	Index	3475	39	2695	44	538	98	1265	39	51			
Routes	Created	3839	39	3243	44	538	98	1265	39	206			
	Branched	3839	39	3057	44	538	98	1265	39	205			
	Selected	918	103	20	122	20	62	35	88	23			
	Prisegoned	4759	0	4146	0	240	0	895	0	0			
Visits	Required	234	44	298	46	172	56	282	40	100			
	Pending	0	2	0	2	2	0	2	2	0			

Plant p1 - Product i1						Plant p1 - Product i2							
Route	Sort value	Distance	Fill ratio	C1	C2	C3	Route	Sort value	Distance	Fill ratio	C1	C2	C3
r1	0.088996	38.824435	0.984962	u452			r104	0.13867	76.26834	1	u501		
r2	0.0633795	42.141396	u115				r105	0.187541	103.1476	1	u249		
r3	0.0636135	42.302952	1	u115	u116		r106	0.219706	120.8381	1	u35	u249	
r4	0.0869378	67.813618	1	u373			r107	0.223672	123.0197	1	u249	u501	
r5	0.002019	61.102635	1	u125			r108	0.245995	135.2974	1	u170		
r6	0.0943924	62.77092	1	u452			r109	0.256897	141.2936	1	u170	u243	
r7	0.0955977	63.672487	1	u116	u452		r110	0.276793	152.2359	1	u169		
r8	0.0956268	63.591129	1	u115	u452		r111	0.279369	153.6527	1	u169	u170	u243
r9	0.0958687	63.752686	1	u115	u116	u452	r112	0.280803	154.4418	1	u169	u243	
r10	0.1006547	66.938349	1	u13			r113	0.283402	155.871	1	u169	u170	

# Conclusions and Future Work



## Conclusions

- Proposed Simultaneous Production-Distribution MILP Model for optimal operational planning of industrial gases supply-chain
  - Multiple products, plants and depots
  - Route generation algorithm
  - Ad hoc production models
- Selection of routes is a critical aspect to reduce the total cost of production and distribution.
- Good quality solutions for industrial size examples obtained in short CPU times.
- Significant potential savings due to better coordination of production and distribution.

## Future work

- Uncertain behavior analysis (electricity prices & customer demands)
  - Stochastic optimization
  - Robust optimization