

Optimal Grade Transitions in a Gas-phase Polymerization Fluidized Bed Reactor

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Introduction

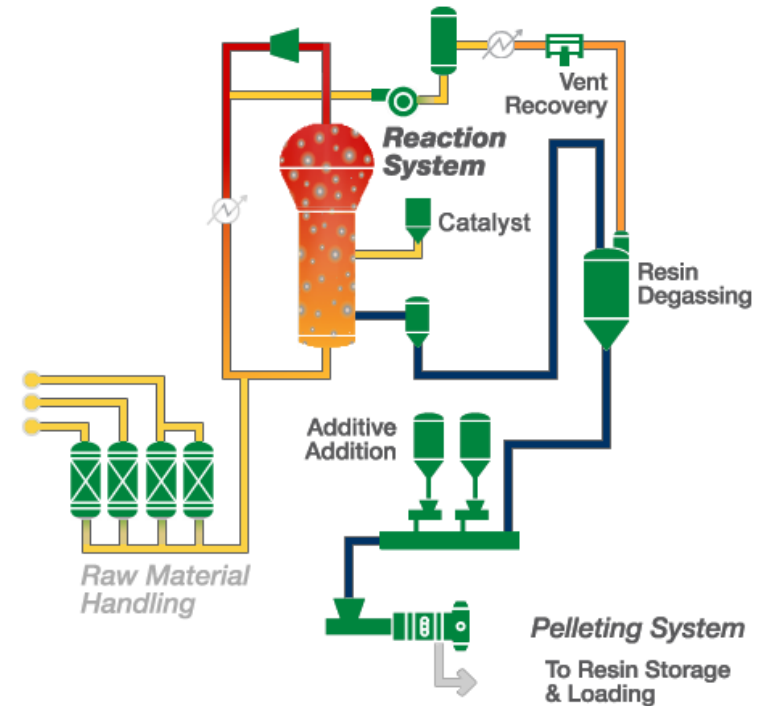
Motivation

Polymer products change frequently.

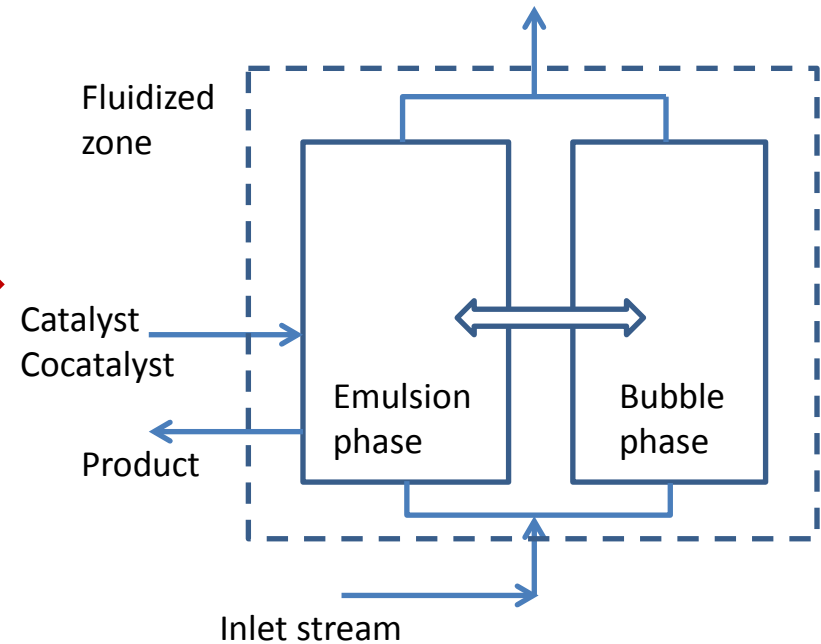
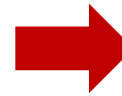
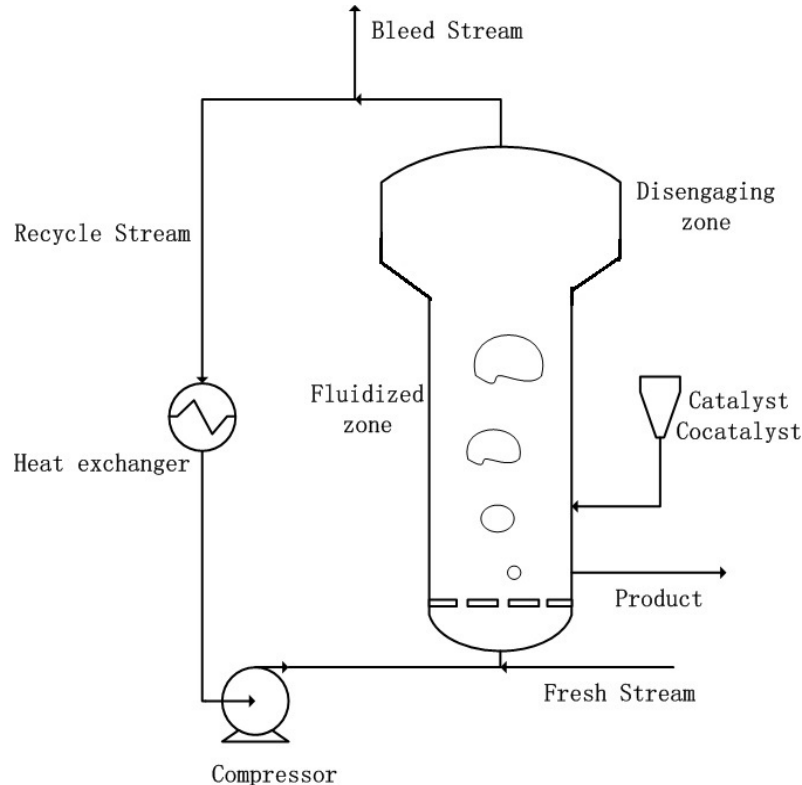
- The transition usually takes hours.
- Tons of off-specification polymers are generated.

Objective

- The objective is to reduce the transition time and off-specification products, while guaranteeing the product property requirements.
- Dynamic optimization is carried out to determine optimal operation sequences in grade transitions.



Fluidized bed reactor (FBR)



Gas feeds:

- C-3 inlet flow
- C-2 inlet flow
- H₂ inlet flow
- N₂ inlet flow

Solid feeds:

- Catalysts
- Cocatalysts

Two-phase model

- Emulsion Phase
 - Solids and gases
 - Minimum fluidization
 - Polymerization reactions
- Bubble Phase
 - Gases only

Polymerization reactions

| Reaction step | Reactant | Reaction | Rate constant |
|-------------------|-------------|---|---------------|
| Site activation | Hydrogen | $C_P + H_2 \rightarrow P_0$ | k_{AH} |
| | Cocatalyst | $C_P + A \rightarrow P_0 + B$ | k_{AA} |
| Chain initiation | Monomer i | $P_0 + M_i \rightarrow P_{1,i}$ | k_{Ii} |
| Chain propagation | Monomer j | $P_{n,i} + M_j \rightarrow P_{n+1,j}$ | k_{Pj} |
| Chain transfer | Hydrogen | $P_{n,i} + H_2 \rightarrow P_0 + D_{n,i}$ | k_{TH} |
| | Monomer j | $P_{n,i} + M_j \rightarrow P_{1,j} + D_{n,i}$ | k_{TMj} |
| | Spontaneous | $P_{n,i} \rightarrow P_0 + D_{n,i}$ | k_{TS} |
| Site deactivation | Spontaneous | $P_{n,i} \rightarrow C_d + D_{n,i}$ | k_{DS} |
| | | $P_0 \rightarrow C_d$ | |

C_P : potential site

P_0 : activated site

C_d : dead site

A: cocatlyst

M_i : monomer i, $i \in \{C_3H_6, C_2H_4\}$

$P_{n,i}$: live polymer with chain length n and end group M_i

$D_{n,i}$: dead polymer with chain length n and end group M_i

Moment model

Live polymer moments:
$$\mu_k = \sum_{n=1}^{\infty} n^k [P_n]$$

Bulk polymer moments:
$$\lambda_k = \sum_{n=1}^{\infty} n^k ([P_n] + [D_n])$$

- First three moments are sufficient to describe some properties, like MFI.
- Instead of listing rate equations of all polymer chains, only equations for leading moments are required.

| Moments | Reaction Rate |
|--------------|---|
| Zero order | $R_{\mu_0} = \sum_{i=1}^{NM} (k_{Ii}[P_0][M_i]) - ((k_{TH} + k_{DH})[H_2] + (k_{TS} + k_{DS}))\mu_0$ $R_{\lambda_0} = \sum_{i=1}^{NM} k_{Ii}[P_0][M_i]$ |
| First order | $R_{\mu_1} = \sum_{i=1}^{NM} (k_{Ii}[P_0][M_i] + k_{Pi}[M_i]\mu_0 + k_{TMi}[M_i](\mu_0 - \mu_1)) - ((k_{TH} + k_{DH})[H_2] + (k_{TS} + k_{DS}))\mu_1$ $R_{\lambda_1} = \sum_{i=1}^{NM} (k_{Ii}[P_0][M_i] + k_{Pi}[M_i]\mu_0 + k_{TMi}[M_i]\mu_0)$ |
| Second order | $R_{\mu_2} = \sum_{i=1}^{NM} (k_{Ii}[P_0][M_i] + 2k_{Pi}[M_i]\mu_1 + k_{TMi}[M_i](\mu_0 - \mu_2)) - ((k_{TH} + k_{DH})[H_2] + (k_{TS} + k_{DS}))\mu_2$ $R_{\lambda_2} = \sum_{i=1}^{NM} (k_{Ii}[P_0][M_i] + 2k_{Pi}[M_i]\mu_1 + k_{TMi}[M_i]\mu_0)$ |

Mass and energy balance in FBR

- Emulsion Phase

$$\frac{d[Y_i]_e}{dt} = \frac{U_e}{H} ([Y_i]_{in} - [Y_i]_e) + \frac{(1-\delta)K_{be}}{\delta\epsilon_{mf}} ([Y_i]_b - [Y_i]_e) + \frac{1-\epsilon_{mf}}{\epsilon_{mf}} R_i - \frac{[Y_i]_e}{H} \frac{dH}{dt}$$

$$\frac{d[S_j]}{dt} = \frac{Q_{in,j}}{V_e(1-\epsilon_{mf})} [S_j]_{in} - \frac{Q_{out}}{V_e} [S_j] + R_j - \frac{[S_j]}{H} \frac{dH}{dt}$$

$$\begin{aligned} \frac{dT_e}{dt} = & \frac{1}{\sum_i V_e \epsilon_{mf} [Y_i]_e C_{p_i} + V_e (1-\epsilon_{mf}) \rho_{pol} C_{p_{pol}}} (U_e A_e \epsilon_{mf} \sum_i [Y_i]_{in} \int_{T_e}^{T_{in}} C_{p_i} dT \\ & + V_e (1-\epsilon_{mf}) R_{pol} \Delta H_{pol} + V_b H_{be} (T_b - T_e) + V_b K_{be} \sum_i ([Y_i]_b - [Y_i]_e) \int_{T_e}^{T_b} C_{p_i} dT) \end{aligned}$$

- Bubble Phase

$$\frac{d[Y_i]_b}{dt} = \frac{U_b}{H} ([Y_i]_{in} - [Y_i]_b) - K_{be} ([Y_i]_b - [Y_i]_e) - \frac{[Y_i]_b}{H} \frac{dH}{dt}$$

$$\frac{dT_b}{dt} = \frac{1}{\sum_i V_b [Y_i]_b C_{p_i}} (U_b A_b \sum_i [Y_i]_{in} \int_{T_b}^{T_{in}} C_{p_i} dT - V_b H_{be} (T_b - T_e))$$

Property predictions

- Empirical correlations for MFI^[1]

$$MFI = a \times (\overline{Mw})^b$$

where the weight average molecular weight, $\overline{Mw} = W \lambda_2 / \lambda_1$
(W is the average molecular weight of one unit in polymers.)

- ODE equations for cumulative composition $\Phi_{C_3H_6}$ ^[2]

$$\frac{d(M_{pol} \Phi_{C_3H_6})}{dt} = -V_e (1 - \varepsilon_{mf}) \phi_{C_3H_6} \sum_i R_i W_i - Q_{out} (1 - \varepsilon_{mf}) (1 - \delta) \Phi_{C_3H_6}$$

where M_{pol} is the mass in the reactor,

W_i is the molecular weight of monomer i ,

$\phi_{C_3H_6}$ is the instantaneous composition of propylene.

[1] Ahmmed S Ibrehem, Mohamed A Hussain, and Nayef M Ghasem. Modified mathematical model for gas phase olefin polymerization in fluidized-bed catalytic reactor. Chemical Engineering Journal, 149(1):353–362, 2009.

[2] C Chatzidoukas, JD Perkins, EN Pistikopoulos, and C Kiparissides. Optimal grade transition and selection of closed loop controllers in a gas-phase olefin polymerization fluidized bed reactor. Chemical Engineering Science, 58(16):3643–3658, 2003.

Polymer grades

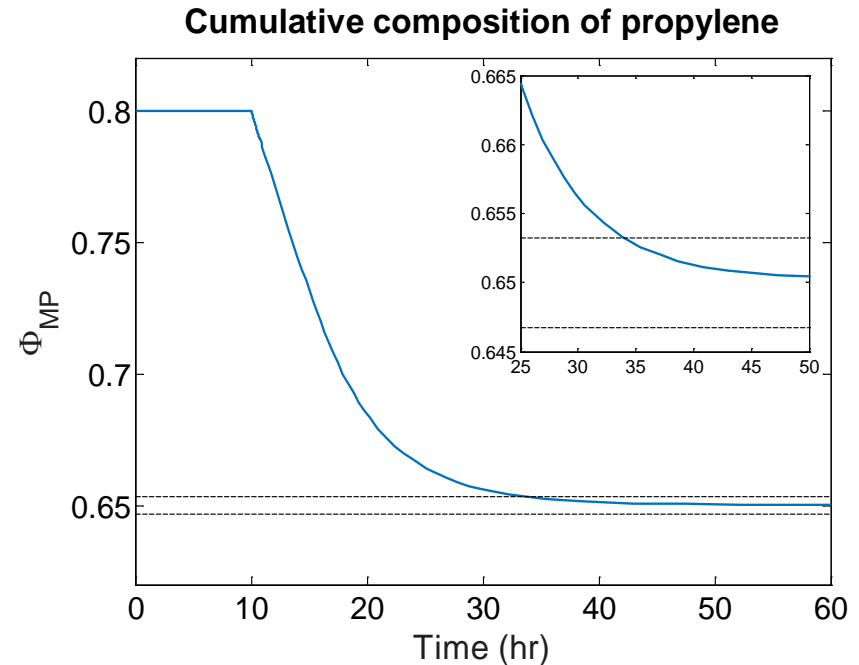
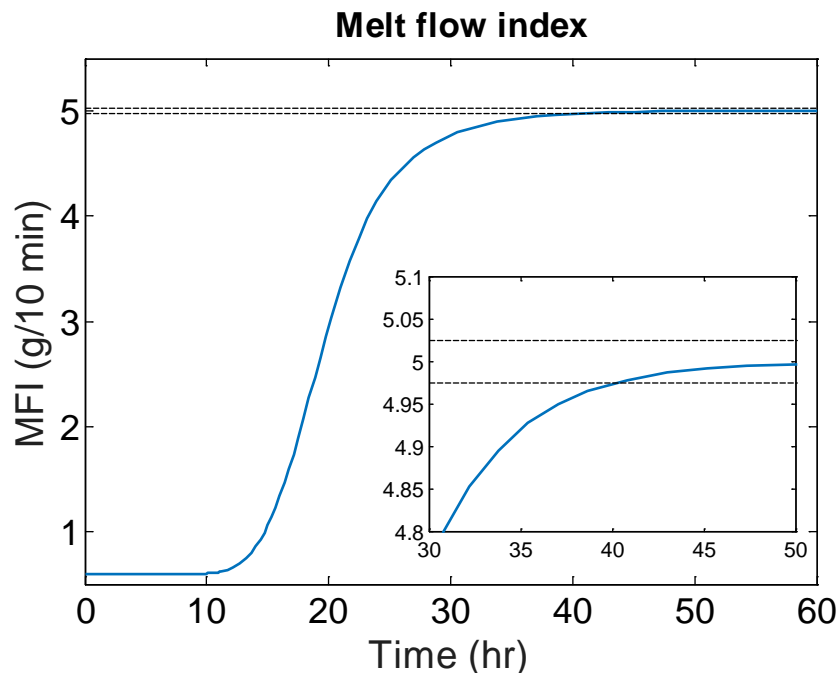
Grade properties and operation conditions for two different grades.

| | | Grade A | Grade B |
|-----------------------|--------------------------------------|-----------------------|-----------------------|
| End-use properties | MFI ($g/10min$) | 0.6 | 5 |
| | $\Phi_{C_3H_6}$ | 0.8 | 0.65 |
| | Production (ton/hr) | 17 | 17 |
| Manipulated variables | C-3 inlet flowrate (m^3/s) | 1.64 | 1.35 |
| | C-2 inlet flowrate (m^3/s) | 1.37 | 2.38 |
| | H_2 inlet flowrate (m^3/s) | 6.60×10^{-2} | 0.23 |
| | N_2 inlet flowrate (m^3/s) | 0.20 | 0.51 |
| | Catalyst inlet flowrate (m^3/s) | 2.22×10^{-4} | 3.79×10^{-4} |
| | Cocatlyst inlet flowrate (m^3/s) | 2.67×10^{-4} | 3.87×10^{-4} |
| | Product outlet flowrate (m^3/s) | 1.04×10^{-2} | 1.07×10^{-2} |
| | Inlet temperature (K) | 346.7 | 344.0 |

The transition from grade A to grade B is studied.

Step response

- The system initially produces polymers in grade A
- At 10 hours, the operation conditions change to grade B.



- The transition ends when the properties reach and stay within a small region around the desired properties.
- The transition time for step change is around **27 hours**.

Optimization formulation

$$\min_{z,u} \int_{t_0}^{t_f} \alpha \|Q - Q^*\|^2 + \beta \|u - u^*\|^2 dt$$

$$\text{s.t.} \quad \frac{dz(t)}{dt} = F(z(t), y(t), u(t), t)$$

$$0 = G(z(t), y(t), u(t), t)$$

$$z^L \leq z(t) \leq z^U$$

$$y^L \leq y(t) \leq y^U$$

$$u^L \leq u(t) \leq u^U$$

Mass/energy balance
Volume change
Cumulative composition

Hydrodynamics
Pressure
MFI

Q: properties (MFI, $\Phi_{\text{C}_3\text{H}_6}$)

z: state variables
(concentrations, moments, temperature)

u: manipulated variables
(feed flowrates, feed temperature)

y: algebraic variables (pressure)

The dynamic optimization problem is solved by a simultaneous approach

Finite element number

| | | | | |
|---------------------------|-----------------------|-----------------------|-----------------------|-----------------------|
| Number of Finite elements | 20 | 40 | 80 | 300 |
| Number of equations | 1.62×10^3 | 3.24×10^3 | 6.48×10^3 | 2.43×10^4 |
| Solve time (sec) | 71.67 | 465.48 | 1726.5 | 5572.8 |
| Iterations | 285 | 691 | 1236 | 948 |
| Scaled objective values | 8.86×10^{-2} | 8.80×10^{-2} | 8.69×10^{-2} | 8.68×10^{-2} |
| Transition time (hr) | 14.1 | 13.0 | 12.3 | 12.3 |

Fewer finite elements → **faster to solve**; larger objective value and longer transition time

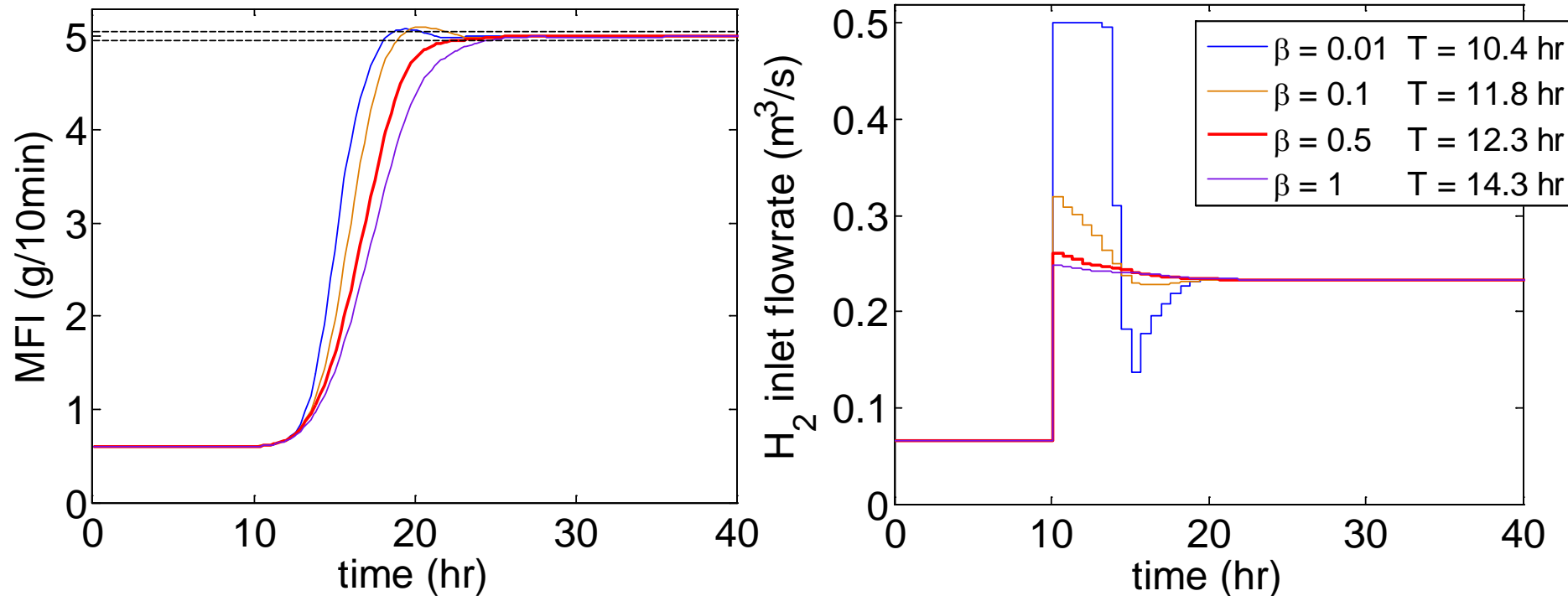
More finite elements → slower to solve; **better objective values and shorter transition time**

✓ **80 finite elements**, considering the optimization results and computational time.

Weight factors

$$\min_{z,u} \int_{t_0}^{t_f} \left\| \frac{Q}{Q^*} - 1 \right\|^2 + \beta \left\| \frac{u}{u^*} - 1 \right\|^2 dt$$

The objective function is scaled. α is fixed to 1 and only β varies.



Small $\beta \rightarrow$ fast transition; severe offset and oscillations

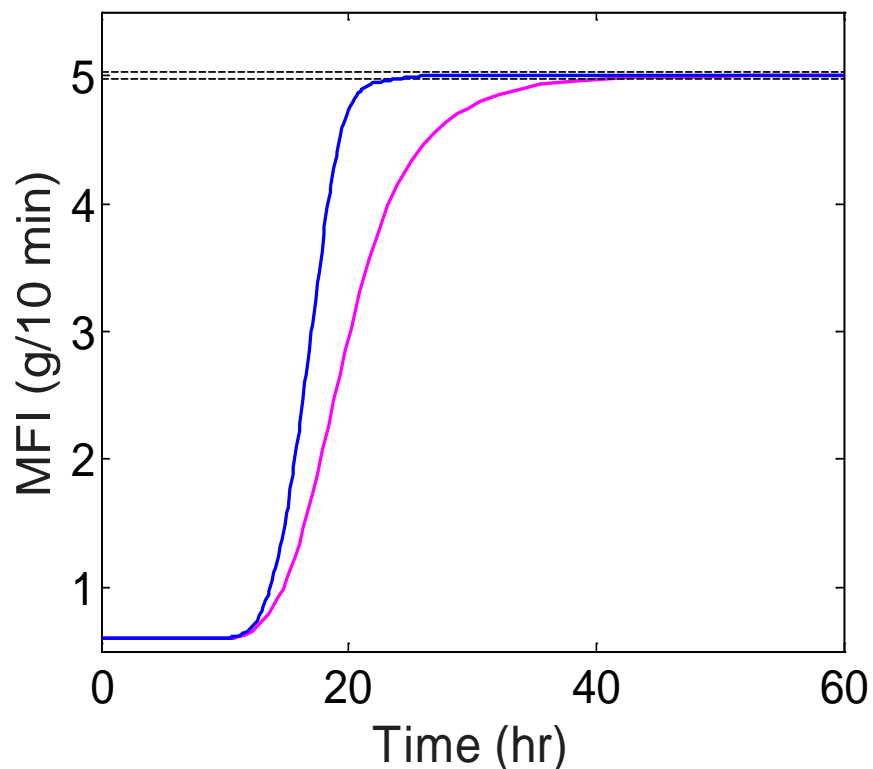
Large $\beta \rightarrow$ slow transition; smooth responses

✓ $\beta=0.5$, considering transition time and smoothness.

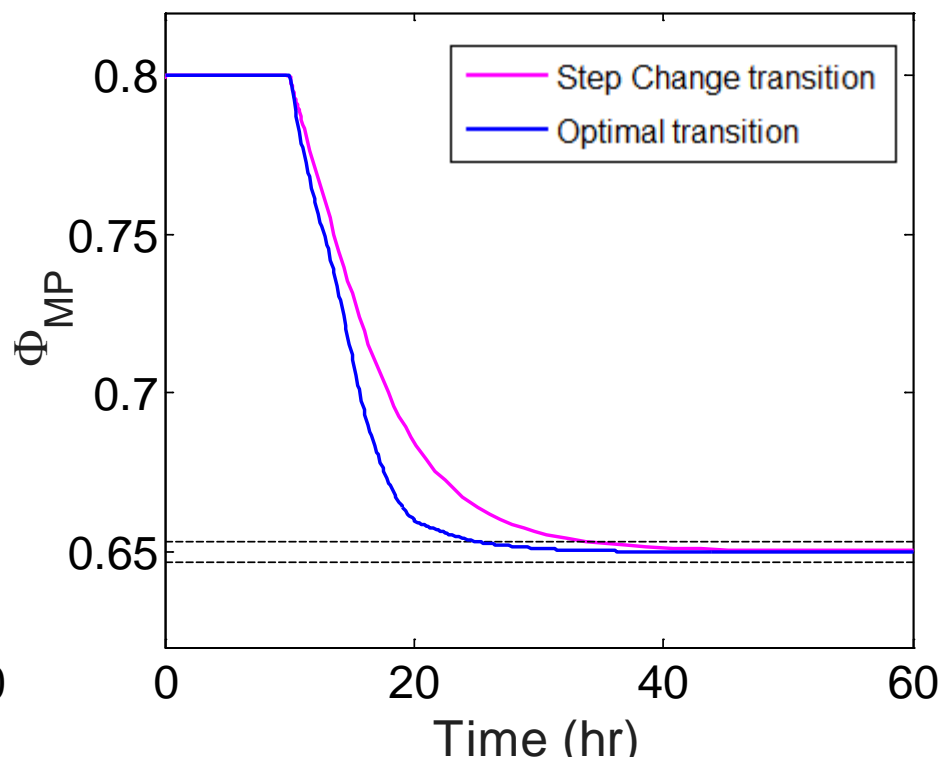
Optimization results --- properties

Run optimization problem with **80 finite elements** and **weight factor $\beta = 0.5$**

Melt flow index



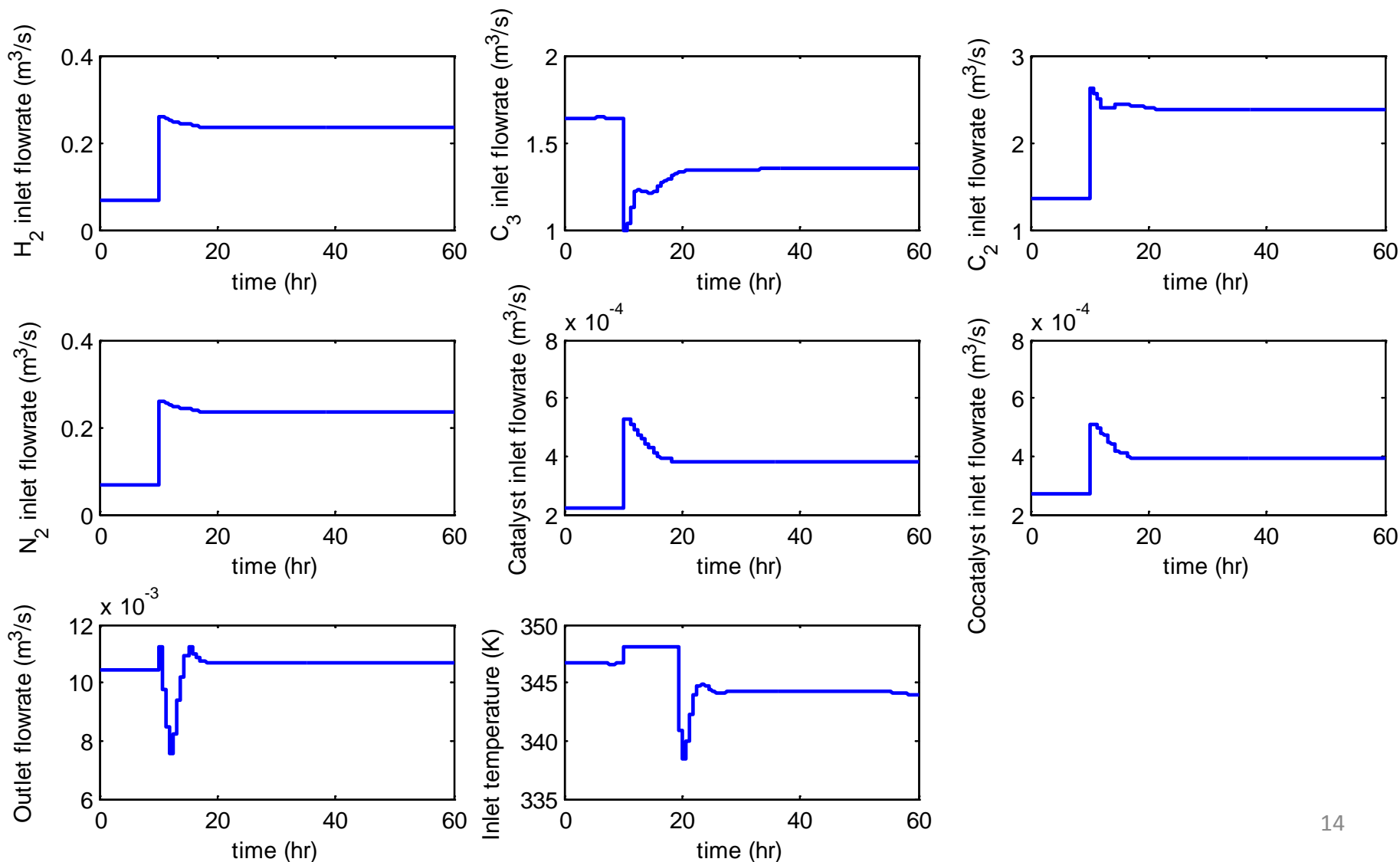
Cumulative composition of propylene



The transition time is cut by **54.4%**. (reduced from 27 hrs to 12.3 hrs).
The production of off-grade polymers is reduced by **54.0%**.

Optimization results --- manipulated variables

Run optimization problem with **80 finite elements** and **weight factor $\beta = 0.5$**



Conclusions and future work

- Developed a dynamic **model** of propylene/ethylene copolymerization in the fluidized bed reactor.
- Simulated the **grade transition** behaviors.
- Solved the **dynamic optimization** problem by a simultaneous method. The transition time is cut down by more than half.
- Considered the effects of **finite element number and weight factors**.

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- Extend the model for multiple site catalysts with site transformation reactions.
 - Implement VLE model to prevent gas phase condensation. Surrogate models may be considered.
 - Modify the objective functions to take off-spec products into account directly.