

# Integrated Scheduling and Dynamic Optimization of Batch Processes Using State Equipment Networks

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- The current status quo of batch scheduling and operations
  - ▶ Batch process scheduling: **recipe-based approaches**
    - ★ Decoupled scheduling and unit operations
    - ★ Dow's practice: **Discrete-time resource-task network**<sup>1</sup>
    - + **Easy (linear) models for scheduling**
    - **Poor process flexibility**
    - **Loss of process profitability**

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- Integration of scheduling and dynamic optimization
  - ▶ Adding value to existing assets
  - ▶ Improving plant **reliability**

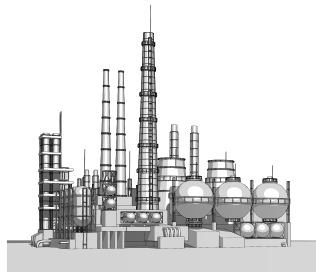
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# Introduction

## Problem description

- Given
  - ▶ A batch plant with existing equipment
  - ▶ A time horizon to make products
  - ▶ Dynamic models of process operations
- Determine
  - ▶ The optimal production schedule
  - ▶ The optimal equipment control strategy
- Via
  - 1 Process representation using the state equipment network(SEN)
  - 2 Mathematical optimization formulation



# Solution Strategy

Integrated optimization based on the SEN

- The SEN represents the process system as a **directed graph** connecting two kinds of nodes

**Material** Feed, intermediate and final products

**Equipment** Process units carrying out operations

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- The integrated formulation

**Objective function** Max **Profit** = **Product sales** - **Material cost** - **Operating cost**

**Constraints**

▶ **Scheduling considerations**

Assignment constraints, material balance, capacity constraints, timing constraints

▶ **Unit operation**

Dynamic first-principle models, limits on controls and states

▶ **Material quality measurement**

Material blending, quality requirements

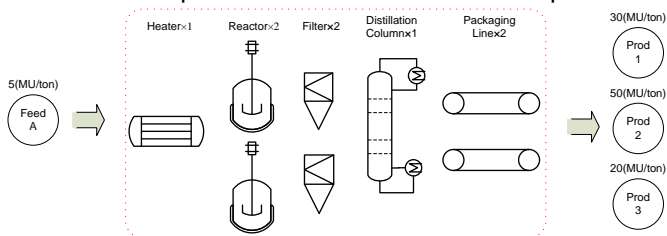
▶ **Auxiliary tightening constraints**

Tightening timing constraints, mass balance of process units

# Case Study

## A jobshop batch plant

- Equipment units and products manufactured in the plant

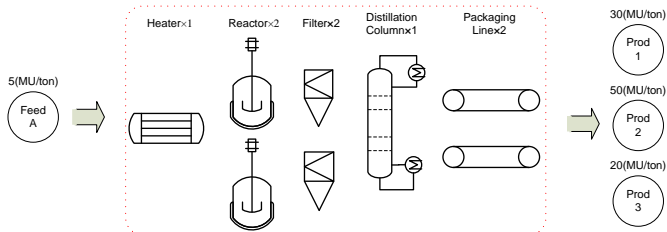




# Case Study

## A jobshop batch plant

- Equipment units and products manufactured in the plant



- Maximizing the net profit within a 10-hour time horizon

Model	Type	Statistics		
		Var.(Discrete) #	Nonlinear Var. #	Cons. #
Recipe-based	MILP	676(90)	0	1079
Integrated	MINLP	4978(90)	2292	12507

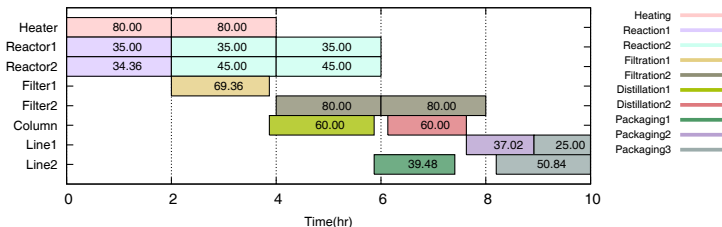
Model	Solution			
	Profit(MU)	CPU time (s)	Node(Best) #	Gap(%)
Recipe-based	1374	0.366	288(199)	0.0
Integrated	1935	9564	5000(1602)	67.9

MILP solved by CPLEX, MINLP solved by SBB(CONOPT)

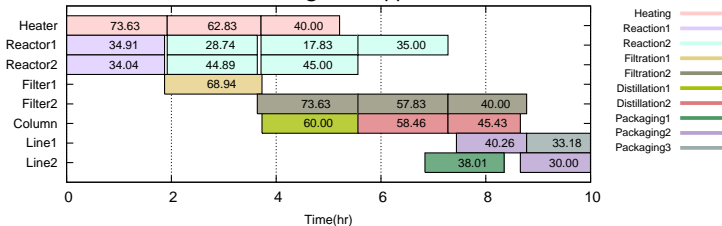
# Case Study

## Optimal production schedules in Gantt charts

### Recipe-based approach



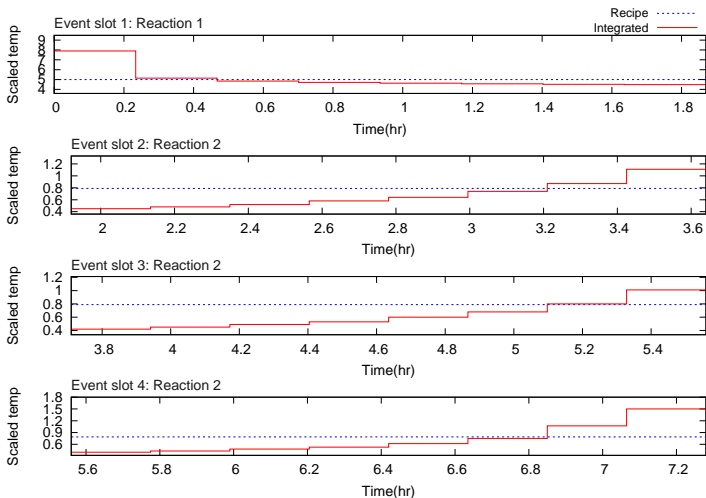
### Integrated approach



# Case Study

## Optimal operating profiles for batch units

- Optimal temperature profiles of *Reactor 1*



Dynamic profiles also obtained for *Reactor 2* and *Distillation Column*

- Concluding remarks
  - ▶ The *state equipment network* representation of batch processes
  - ▶ An optimization formulation for the *integration* of scheduling and dynamic optimization

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- Future work

Off-line→On-line

- ▶ Alternative scheduling formulations
- ▶ Data-driven dynamic models

- Concluding remarks
  - ▶ The *state equipment network* representation of batch processes
  - ▶ An optimization formulation for the *integration* of scheduling and dynamic optimization

- Future work

Off-line→On-line

- ▶ Alternative scheduling formulations
  - ▶ Data-driven dynamic models
- Thank you

I am glad to take questions...