Optimization of Maritime Transportation

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M. Christiansen, K. Fagerholt, B. Nygreen and D. Ronen (2013). Ship routing and scheduling in the New Millennium. EJOR, 228, 467-483


Outline

• Introduction to maritime transportation
• Maritime cargo routing
• Maritime inventory routing
• Trends relevant for ship routing and scheduling
• Concluding remarks
Outline

- Introduction to maritime transportation
- Maritime cargo routing
- Maritime inventory routing
- Trends relevant for ship routing and scheduling
- Concluding remarks
Cargo ships

- Tankers
  - Carry liquids in bulk
- Bulk carriers
  - Carry dry bulk commodities
- Reefers
- Liquefied gas carriers
- Ro-ro ships
- Container ships
- General cargo vessels
- Etc…

Photo: Gary Blakeley
Cargo ships - ports

• Ships operate between ports
  – Loading (pickup) and unloading (delivery)
  – Supply of fuel, fresh water, etc…

• Physical limitations impose compatibility constraints between ships and ports
  – Draft, length, etc…

• Ships pay port fees

• Transhipment of containers

• Storages placed near ports

• Limited number of berths, cranes or pipes

Port operations are not focused here
Maritime transportation - key figures

- **Major mode of international trade**
  - Around 90% of world trade is carried by the international shipping industry. ([http://www.ics-shipping.org/shipping-facts/shipping-and-world-trade](http://www.ics-shipping.org/shipping-facts/shipping-and-world-trade))

- **Monopoly on transportation of large volumes between continents (deep sea shipping)**

- **Major role in domestic trades (short sea shipping) for countries with**
  - Long shoreline (e.g. Norway)
  - Many rivers (e.g. USA)
  - Many islands (e.g. Greece)
World fleet

compiled from UNCTAD, 2013
(million dwt)

- Oil Tankers
- Dry Bulk
- General Cargo
- Container
- Other
- Total
Compiled from UNCTAD, 2013
(millions of tons loaded)

- Oil&Gas
- Main bulks
- Other dry cargo
- Container
- Total
Importance of proper ship routing

- Ships involve major investments and high operating costs:

- The shipping industry has experienced a considerable change (consolidation in the manufacturing sector, increasing competition, profit margins reduced, mergers and pooling, extended logistic tasks)

- Good planning is crucial for survival:
  - Reducing costs
  - Increasing revenue by carrying spot cargoes
  - Giving important positive environmental effects

- Relatively little OR-work has been done in ship routing

**Example: A VLCC, 200,000 dwt:**

- Building cost: 100 mill. USD
- Daily TC rate: 70,000 USD
- Daily fuel costs: 50,000 USD
- Port fee: 100,000 USD
- Value of one cargo: 100 mill. USD

*(figures only roughly estimated)*
Growth in number of publications

- General surveys on maritime ship routing and scheduling:
    - 3 decades, 40 references
    - 1 decade, 40 references
    - 1 decade, 80 references
  - Christiansen, Fagerholt, Nygreen and Ronen, *EJOR* (2013)
    - 1 decade, 130 references
Basic modes of operation (Lawrence ’72)

• **Industrial shipping**
  – Shipper(cargo owner) controls the fleet of vessels (owned or on TC)
  – Must ship the total demand while minimizing costs
  – Decisions: Routing and scheduling
  – Vertically integrated companies

• **Tramp shipping**
  – Combination of contract and optional spot cargoes
  – Ships follow the available cargoes, similar to a taxi service
  – Decisions: Routing/scheduling and selection of spot cargoes
  – Maximize profit

• **Liner shipping**
  – Ships follow a published schedule, similar to a bus line
  – Container, ro-ro and general cargo vessels
Planning levels

• **Strategic planning level (1-20 years)**
  – Market and trade selection (Contract evaluation)
  – Fleet size and mix decisions
  – Network design in liner shipping

• **Tactical planning level (1 week – 1 year)**
  – Ship scheduling for industrial and tramp shipping
  – Port management (inventory management, berth scheduling, …)
  – Fleet deployment in liner shipping
  – Empty container distribution
  – Berth scheduling – Allocation of ships to berths

• **Operational planning (1 day – 1 week)**
  – Environmental routing (Weather routing and ocean currents)
  – Speed selection for a sailing leg
  – Ship loading (Container stowage, Crane scheduling)
  – Booking of single orders in liner shipping
Outline

• Introduction to maritime transportation

  • Maritime cargo routing

• Maritime inventory routing

• Trends relevant for ship routing and scheduling

• Concluding remarks
Maritime cargo routing*

- Routing and scheduling of bulk cargoes
- Tactical planning level with planning horizon from 1 week to 1 year
- Focus on tramp shipping
- A cargo routing problem in industrial shipping can be obtained by including mandatory cargoes only
- Models and solution methods
- Extensions and variants

*Al-Khayyal and Hwang (2007) Inventory constrained maritime routing and scheduling for multi-commodity liquid bulk, part i: Applications and model. EJOR.*
Tramp shipping: Planning process

- Mix of mandatory contract cargoes and optional spot cargoes
- Several daily requests for spot cargoes
- Negotiate spot cargoes and schedule the fleet
  - Continuous and interwoven process
- Objective: Maximize profit
- Core business for many shipping companies
Maritime cargo routing

- Heterogeneous fleet of ships with different
  - Capacity
  - Speed
  - Initial position

- Set of cargoes to be lifted
  - Load and discharge port
  - Time windows
  - Quantity
  - Freight revenue

- Mix of contract (C) and optional spot (S) cargoes

<table>
<thead>
<tr>
<th>Cargo</th>
<th>From</th>
<th>To</th>
<th>Quantity [ton]</th>
<th>Time window</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 (C)</td>
<td>Boston</td>
<td>Milford Haven</td>
<td>30.000</td>
<td>4/11-08 – 11/11-08</td>
</tr>
<tr>
<td>2 (C)</td>
<td>New York</td>
<td>Antwerp</td>
<td>30.000</td>
<td>5/11-08 – 12/11-08</td>
</tr>
<tr>
<td>3 (S)</td>
<td>New York</td>
<td>Milford Haven</td>
<td>20.000</td>
<td>5/11-08 – 12/11-08</td>
</tr>
</tbody>
</table>
### Example: Manual planning worksheet

<table>
<thead>
<tr>
<th>UK/CONT</th>
<th>MEDIT</th>
<th>CARIB</th>
<th>US/GULF</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cecilia&lt;br&gt;Antwerp 2/11-07&lt;br&gt;Catharina&lt;br&gt;Antwerp 7/11-07</td>
<td>Suzanna&lt;br&gt;Jose 15/10-07</td>
<td>Alberta&lt;br&gt;Boston 4/11-07&lt;br&gt;Maria&lt;br&gt;Charleston 23/10-07</td>
<td></td>
</tr>
</tbody>
</table>
Basic Maritime cargo routing

- **Objective:** Maximize profit (gross margin)
  - Revenue from transported cargoes – variable sailing costs (fuel costs, port costs, canal costs, etc.)

- **Constraints**
  - All mandatory contract cargoes must be transported once
  - Optional spot cargoes can be transported at most once
  - Routing constraints
  - Load management on board the ship
  - Time constraints
  - Ship capacity constraints

- **Maritime Pickup and Delivery Problem with Time Window (PDPTW)**
Maritime cargo routing model: Notation

- \( N \) is the total number of cargoes in the planning horizon

- Transporting cargo \( i \) generates a revenue \( P_i \)

- Node \( N+i \) is the delivery (unloading) node corresponding to the pickup (loading) node \( i \) for cargo \( I \)

- Quantity of cargo \( i \) is \( Q_i \) while capacity of ship \( v \) is \( K_v \)
Maritime cargo routing model (1:2)

\[
\begin{align*}
\text{max} & \quad \sum_{i \in \mathcal{N}^C} P_i + \sum_{i \in \mathcal{N}^O} P_i y_i - \sum_{v \in V} \sum_{(i,j) \in \mathcal{A}_v} C_{ijv} x_{ijv}, \\
\text{Revenue – variable costs} & \\
\text{Subject to:} & \\
\sum_{v \in V} \sum_{j \in \mathcal{N}_v} x_{ijv} = 1, & i \in \mathcal{N}^C, & \text{Contract cargoes must be transported once} \\
\sum_{v \in V} \sum_{j \in \mathcal{N}_v} x_{ijv} - y_i = 0, & i \in \mathcal{N}^O, & \text{Optional cargoes may be transported once} \\
\sum_{j \in \mathcal{N}_v} x_{o(v)jv} = 1, & v \in \mathcal{V}, & \\
\sum_{j \in \mathcal{N}_v} x_{ijv} - \sum_{j \in \mathcal{N}_v} x_{jiv} = 0, & v \in V, i \in \mathcal{N}_v \backslash \{o(v), d(v)\}, & \text{Routing constraints} \\
\sum_{i \in \mathcal{N}_v} x_{id(v)v} = 1, & v \in \mathcal{V}, & 
\end{align*}
\]
### Maritime cargo routing model (2:2)

<table>
<thead>
<tr>
<th>Constraint</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>( l_{iv} + Q_j - l_{jv} - K_v (1 - x_{ijv}) \leq 0 ), ( v \in V, (i,j) \in A_v</td>
<td>j \in N_v )</td>
</tr>
<tr>
<td>( l_{iv} - Q_j - l_{n+j,v} - K_v (1 - x_{i,n+j,v}) \leq 0 ), ( v \in V, (i, n+j) \in A_v</td>
<td>j \in N_v )</td>
</tr>
<tr>
<td>( \sum_{j \in N_v} Q_i x_{ijv} \leq l_{iv} \leq \sum_{j \in N_v} K_v x_{ijv} ), ( v \in V, i \in N_v )</td>
<td>Ship capacity constraints</td>
</tr>
<tr>
<td>( 0 \leq l_{n+i,v} \leq \sum_{j \in N_v} (K_v - Q_i) x_{n+i,jv} ), ( v \in V, i \in N_v )</td>
<td>Ship capacity constraints</td>
</tr>
<tr>
<td>( t_{iv} + T_{ip}^v + T_{ijv} - t_{jv} - M_{ijv} (1 - x_{ijv}) \leq 0 ), ( v \in V, (i,j) \in A_v )</td>
<td>Time constraints</td>
</tr>
<tr>
<td>( \sum_{j \in N_v} x_{ijv} - \sum_{j \in N_v} x_{n+i,jv} = 0 ), ( v \in V, i \in N_v )</td>
<td>Cargo coupling constraints</td>
</tr>
<tr>
<td>( t_{iv} + T_{ip}^v + T_{i,n+i,v} - t_{n+1,v} \leq 0 ), ( v \in V, i \in N_v )</td>
<td>Precedence constraints</td>
</tr>
<tr>
<td>( T_{iv} \leq t_{iv} \leq \bar{T}_{iv} ), ( v \in V, i \in N_v )</td>
<td>Time windows</td>
</tr>
<tr>
<td>( l_{iv} \geq 0 ), ( v \in V, i \in N_v )</td>
<td></td>
</tr>
<tr>
<td>( x_{ijv} \in {0,1} ), ( v \in V, (i,j) \in A_v )</td>
<td></td>
</tr>
<tr>
<td>( y_i \in {0,1} ), ( i \in N^0 ).</td>
<td></td>
</tr>
</tbody>
</table>
Maritime cargo routing: Path flow model

\[
\begin{align*}
\max & \sum_{i \in N^C} P_i + \sum_{i \in N^O} P_i y_i - \sum_{v \in V} \sum_{r \in R_v} C_{vr} x_{vr} \\
\sum_{v \in V} \sum_{r \in R_v} A_{ivr} x_{vr} &= 1 \quad \forall i \in N^C \\
\sum_{v \in V} \sum_{r \in R_v} A_{ivr} x_{vr} - y_i &= 0 \quad \forall i \in N^O \\
\sum_{r \in R_v} x_{vr} &= 1 \quad \forall v \in V \\
x_{vr} &\in \{0,1\} \quad \forall v \in V, r \in R_v
\end{align*}
\]

- \(N^C\) - Set of contracted cargoes, \(i\)
- \(N^O\) - Set of optional spot cargoes, \(i\)
- \(V\) - Set of ships, \(v\)
- \(R_v\) - Set of routes for ship \(v, r\)
- \(P_i\) - Revenue for transporting cargo \(i\)
- \(C_{vr}\) - Cost of sailing route \(r\) with ship \(v\)
- \(A_{ivr}\) - \(1\) if route \(r\) for ship \(v\) services cargo \(i\)
- \(x_{vr}\) - \(1\) if ship \(v\) sails route \(r\)
- \(y_i\) - \(1\) if spot cargo \(i\) is transported
Maritime cargo routing: Solution methods

• Some existing research:
  – Column generation based on path-flow model (a priori\(^1\)) or delayed\(^2\))
  – Multi-start local search heuristic\(^3\)). Unified tabu search heuristic\(^4\))
  – Variable neighborhood search heuristic\(^5\))

• Both 3) and 4) are implemented as solvers in the DSS TurboRouter

1) Fagerholt and Christiansen (2000). A combined ship scheduling and allocation problem. JORS
Planning flexibility

However, in real life the planner often has more flexibility than modelled in the basic tramp cargo routing and scheduling problem...

... thus the focus has recently been on model extensions that reflect common situations in tramp cargo routing
Maritime PDPTW with Split Loads (SL)

- Split loads - More than one ship can transport one cargo
- Splitting loads may
  - increase port costs
  - reduce sailing costs
  - give business opportunities (adding more spot cargoes to the solution)
- However, splitting loads interact with the routing decisions and affect several ships
- More interesting in deep-sea shipping than short-sea shipping. Why?
  - Sailing costs dominate port costs in deep-sea shipping
Example: Maritime PDPTWSL

30000

35000

50000

60000

www.ntnu.no
Example: Maritime PDPTWSL
Example: Maritime PDPTWSL
Example: Maritime PDPTWSL
Example: Maritime PDPTWSL

30000

35000

(too late)

15000

50000

60000
Example: Maritime PDPTWSL
Example: Maritime PDPTWSL
Maritime PDPTWSDL: Models and methods

- In arc flow model: New load variable \( q_{iv} \) and new load quantity constraints
- A priori column generation\(^1\): Cargo splitting is decided in master problem
- Branch-and-price method\(^2\)
  - Columns for all routes with optimal quantities decided in the master problem
  - Columns including routes and delivery patterns (best)
- Large neighbourhood search heuristic\(^3\)
- Testing shows huge effect on economic result by utilizing split loads

\(^1\) Andersson, Christiansen and Fagerholt (2011) The maritime pickup and delivery problem with time windows and split loads. INFOR
\(^2\) Stålhane, Andersson, Christiansen, Cordeau, Desaulniers (2012) Branch-price-and-cut for a maritime pickup and delivery problem with split loads. COR.
\(^3\) Korsvik, Fagerholt and Laporte (2011) A large neighbourhood search heuristic for ship routing and scheduling with split loads. COR
Complex maritime cargo routing

- Flexible cargo quantities
- Soft time windows
- Restricted opening hours in port
- Speed optimization
- Stowage considerations
- Bunkering decisions
- Dry-docking decisions
- Fleet size and mix
- Considering uncertainty
  - Modelling of market opportunities (TC and spot cargo rates fluctuate)
  - Sailing time and time spent in ports
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Maritime inventory routing

• Often, inventories exist at the loading and unloading ports of the sailing leg

• When one actor (producer, consumer or shipping company) has the responsibility for both transportation and inventories
  ➢ Maritime inventory routing problem (MIRP)
Basic MIRP:

Design routes and schedules that minimize the transportation cost without interrupting production and consumption of a single product.
Basic MIRP: Inventory management

- Single product
- Inventory storages in all ports
- Production/consumption rates are constant in time
- Port $i$, visit number $m$: port visit $(i,m)$
Basic MIRP: Routing and Scheduling

- Heterogeneous fleet of ships
- Generate routes including information about time to start service and (un)loading quantities
- Partial (un)loading, such that several (un)loading ports can be visited in succession

Geographical route: P1→D2→D1→P2→D1→P2→D2

Schedule: T1 T2 T3 T4 T5 T6 T7

Quantity: Q1 Q2 Q3 Q4 Q5 Q6 Q7
Basic MIRP: Example

Inventory port 3

1(U) 3(U) 4(L)

2(L) 5(L)

Load ship 2

Load ship 1

www.ntnu.no
Comparisons to other routing problems

- MIRP is different from maritime cargo routing due to
  - The number of visits at a node is predetermined
  - The quantity loaded/unloaded is normally fixed
  - Predefined pickup and delivery pair
    for maritime cargo routing

- MIRP is different from road-based IRP due to
  - Often one central supplier (depot) with large inventory capacities and many customers consuming a small amount
  - Asymmetry between each type of inventory
  - Small quantities are delivered compared to the maritime IRP
  - Finite planning horizon
    for road-based IRP
Basic MIRP: Model description

- Minimise transportation and port costs
- Each port visit is made at most once
- Routing constraints
- Scheduling constraints
- Load management on board the ship
- Ship capacity constraints
- Inventory balance constraints
- Inventory capacity constraints
Basic MIRP: Path flow model (1:2)

- **Master Problem**
  - Production / consumption rate: \( R_i \)
  - Inventory management at port visit \((i,m), S_{im}\)

- **Path \( r \) for each ship \( v \)**
  - Ship routing
  - Ship scheduling
  - Ship loading/unloading

\[
\begin{align*}
X_{imjvntr} \lambda_vr \\
T_{imv} \lambda_vr \\
Q_{imv} \lambda_vr
\end{align*}
\]
Basic MIRP: Path flow model (2:2)

\[
\min \sum_{v \in V} \sum_{r \in R_v} C_{vr} \lambda_{vr},
\]

\[
\sum_{v \in V} \sum_{r \in R_v} A_{imv} \lambda_{vr} \leq 1, \quad \forall i \in N, m \in M_i,
\]

Port visit

\[
s_{i(m-1)} + \sum_{v \in V} \sum_{r \in R_v} \left[R_i(T_{imv} - T_{i(m-1)v}) - I_i Q_{i(m-1)v}\right] \lambda_{vr} - s_{im} = 0, \quad \forall i \in N, m \in M_i,
\]

Inventory balance

\[
S_i \leq s_{im} \leq \bar{S}_i, \quad \forall i \in N, m \in M_i,
\]

Inventory limits

\[
\sum_{r \in R_v} \lambda_{vr} = 1, \quad \forall v \in V,
\]

Convexity

\[
\sum_{r \in R_v} X_{imjnv} \lambda_{vr} \in \{0,1\}, \quad \forall i \in N, m \in M_i,
\]

\[
\lambda_{vr} \geq 0, \quad \forall v \in V, r \in R_v.
\]
Basic MIRP: Solution methods (1:4)

- Very complex problem to solve due to high degree of freedom
  - No predetermined number of port visits,
  - Variable (un)loading quantities
  - No pickup and delivery pairs,
  - No time windows for arrival
  - Problem specific issues
Basic MIRP: Solution methods (2:4)

- Branch-and-cut methods
  - Agra, Andersson, Christiansen, Wolsey (2013). A maritime inventory routing problem: Discrete time formulations and valid inequalities. *Networks*
  - Furman, Song, Kocis, McDonald, Warrick (2011) Feedstock routing in the ExxonMobil downstream sector. * Interfaces*

*Reformulating the arc flow formulations: Fixed charge network flow formulations with side constraints reduces the integrality gaps from 83% in average to 36% in average. Cuts reduce the gaps to 6% in average.*
Basic MIRP: Solution methods (3:4)

- Several branch-and-price approaches
  - Christiansen (1999). Decomposition of a Combined Inventory and Time Constrained Ship Routing Problem, Transportation Science
  - Rakke, Andersson, Christiansen, Desaulniers (2014). A new formulation based on customer delivery patterns for a maritime inventory routing problem. Transportation Science

- Columns: ship routes and schedules including information about (un)load quantities
Heuristics

- Dauzére-Pérès, Nordli, Olstad, Haugen, Koester, Myrstad, Teistklub, Reistad. (2007). Omya Hustadmarmor optimizes its supply chain for delivering calcim carbonate slurry to European paper manufacturers. *Interfaces*
- Goel, Furman, Song, El-Bakry (2012). Large neighborhood search for LNG inventory routing. *Journal of Heuristics*
- Rakke, Stålhane, Moe, Andersson, Christiansen, Fagerholt, Norstad (2011). “A rolling horizon heuristic for creating a liquefied natural gas annual delivery program”. *Transportation Research C*
- Stålhane, Rakke, Moe, Andersson, Christiansen, Fagerholt (2012). A Constructive and Improvement Heuristic for a Liquefied Natural Gas Inventory Routing Problem. *Computers and Industrial Engineering*
Complex MIRPs

- Multiple products
- Constant, time varying or variable consumption/production rate
- Inventory constraints in either production or consumption ports
  - Contracts with given quantities and time windows in the other type of ports
- Combined inventory routing and tramp shipping
- Combining inventory routing with other planning aspects
  - Consider larger parts of the supply chain (for instance include production)
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Business trends (1:3)

• Mergers and collaborations
  – To increase market power and gain flexibility in the services
  – Larger fleet and more complex transportation pattern

• New generation of planners
  – With computer experience and more academic background

• Focus on supply chains (SC)
  – Integration along the SC (cargo owner and shipping company)
  – Vendor managed inventory systems
  – Shipping integrated into a multimodal door-to-door SC

• An increasing LNG activity
  – Challenging inventory routing problems
Business trends

• Oversupply of tonnage
  – Years with global financial crisis. Economic situation has brightened, but multiple risks threaten for a stable world economy
  – Slow steaming and use of less costly paths

• Global climate changes
  – Increased accessibility in the Arctic region

• External conditions changes rapidly
  – Planning problems changes
Business trends

- Stricter regulations for emissions of greenhouse gases and Emission Control Area (ECA) regulations
  - Use different fuels when sailing inside and outside ECAs
  - Sailing route options between two ports
  - Sailing speed optimization (third power relationship between bunker fuel consumption and speed)
Maritime transport research trends (1:2)

- Number of maritime transport (MT) articles is increasing
- Most MT articles present special versions of basic problems with tailor-made solution methods
- Several benchmark suites have appeared
  - MIRPLib (http://mirplib.scl.gatech.edu/),
  - LINER-LIB (http://linerlib.org/)
  - Library for tramp and industrial ship routing and scheduling (http://iot.ntnu.no/users/larsmahv/benchmarks/)
- Both exact and heuristic solution methods
- Now, also more theoretical models and basic research that are less grounded in real operations
Maritime transport research trends (2:2)

- MIRP, LNG and offshore supply vessel routing have attracted increasing attention
- Fast growth of the containership fleet
  - Similar growth in research on liner network design and related topics
- Strategic planning issues: fleet size and mix (fleet renewal), contract evaluation
- Varying price of bunker fuel and new environmental regulations
  - Sailing speed (third power relationship between bunker fuel consumption and speed)
  - Alternative routes between two ports
  - Affect planning at strategic, tactical and operational level
- Dynamic and stochastic maritime ship routing and scheduling
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Concluding remarks

- Focused on ship routing and scheduling
- Ship scheduling has high potential for improvements by optimizing fleet utilization (a few % - 25 %)
- Still many shipping companies build their complete routes and schedules manually
- A few DSSs are described in the literature
- An increasing number of publications and groups working on maritime transportation problems
- Rich real problems and external conditions changes rapidly
- Many remaining planning problems to consider
- Need for more research on models, theory and solution methods
Optimization of Maritime Transportation

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